

EEL 3135 – Quiz 5  
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20 minutes close book

By signing my name below, I declare that I have not given or received help from others during the quiz.

Name: SOLUTION, ID #: \_\_\_\_\_

Please answer in the space provided (1 question)

1- The transfer function of a second order IIR filter is

$$H(z) = \frac{12 + 24z^{-1}}{12 + 13z^{-1} + 3z^{-2}}$$

Consider all initial conditions zero.

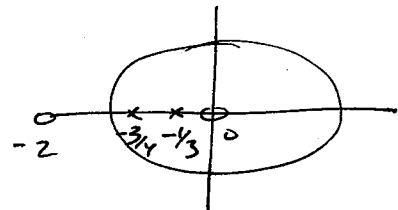
- Draw the pole-zero plot.
- Find the impulse response of the system.

You will need the following relation  $a^n u(n) \leftrightarrow \frac{1}{1-az^{-1}}$

$$12z^2 + 13z + 3 = 0$$

$$z = -\frac{1}{3}, -\frac{3}{4}$$

$$a) \quad H(z) = \frac{12z^2 + 24z}{(4z+3)(3z+1)} = \frac{1+2z^{-1}}{\left(1+\frac{3}{4}z^{-1}\right)\left(1+\frac{1}{3}z^{-1}\right)}$$



$$b) \quad H(z) = \frac{1+2z^{-1}}{\left(1+\frac{3}{4}z^{-1}\right)\left(1+\frac{1}{3}z^{-1}\right)} = \frac{A}{\left(1+\frac{3}{4}z^{-1}\right)} + \frac{B}{\left(1+\frac{1}{3}z^{-1}\right)}$$

$$A = H(z) \left(1+\frac{3}{4}z^{-1}\right) \Big|_{z=-\frac{3}{4}} = -3$$

$$B = H(z) \left(1+\frac{1}{3}z^{-1}\right) \Big|_{z=-\frac{1}{3}} = 4$$

$$\text{So } H(z) = \frac{-3}{\left(1+\frac{3}{4}z^{-1}\right)} + \frac{4}{1+\frac{1}{3}z^{-1}} \implies h(n) = -3 \left(\frac{3}{4}\right)^n u(n) + 4 \left(\frac{-1}{3}\right)^n u(n)$$